

EECS 16B

# Designing Information Devices and Systems II

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Department of Electrical Engineering and Computer Science

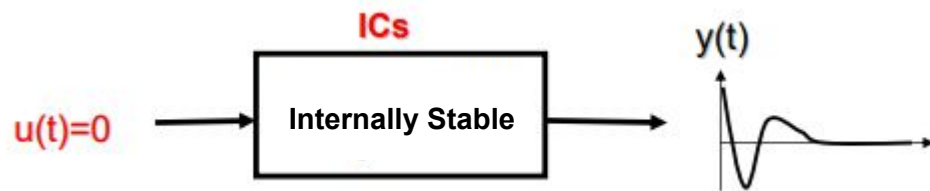
# Announcements

- Please complete our mid-semester survey, due Monday 3/18 @11:59pm

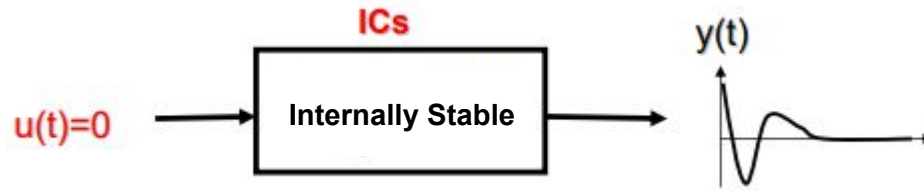
# Today

- Review - stability
- Controllability
  - Reachability

# State Space (“Internal”) Stability



# State Space (“Internal”) Stability



System may be:

- stable
- unstable
- marginally stable

# BIBO Stability



# BIBO Stability



System may be:

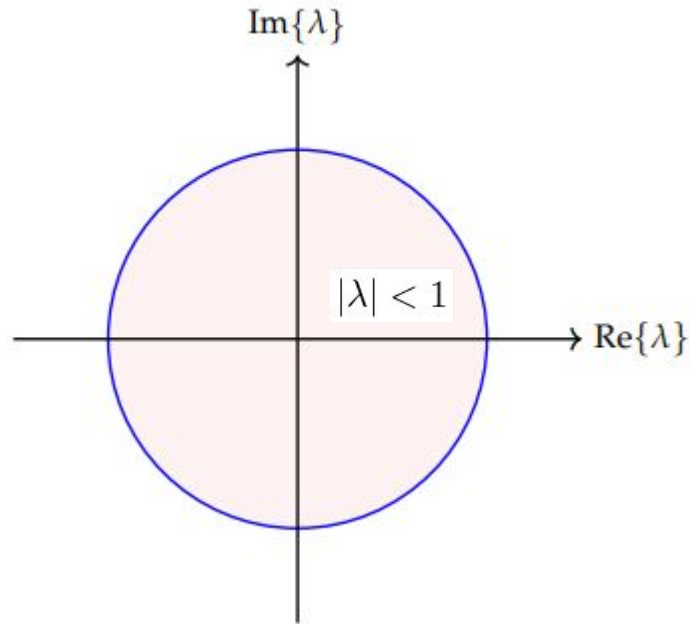
- stable
- unstable

To determine if a system is stable, one must look at:

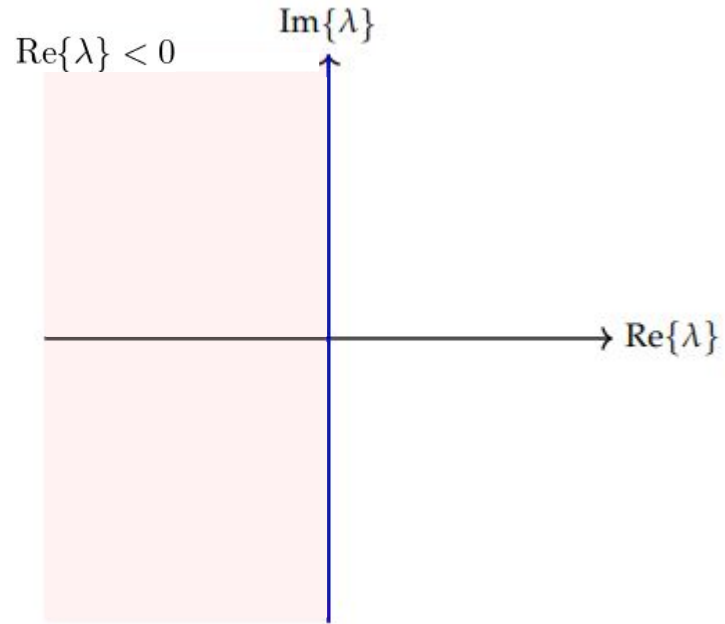
1. the **A** matrix only
2. the **B** matrix only
3. both the **A** and **B** matrices
4. the **A** and **B** matrices for BIBO stability but only the **A** matrix for internal stability



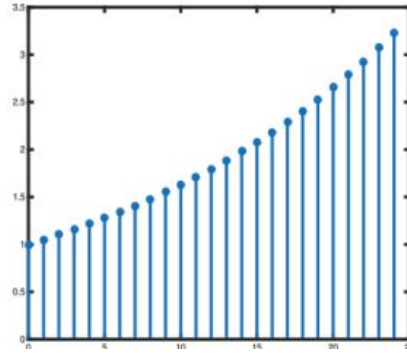
# Stability - Discrete Time System



# Stability - Continuous Time System



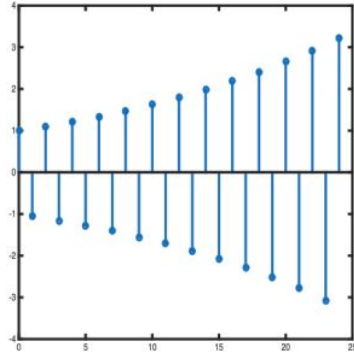
A real-valued DT system generates the following state trajectory:



The above response is associated with which of the following:

1. a negative real eigenvalue  $\lambda$ , with  $|\lambda| > 1$
2. a positive real eigenvalue  $\lambda$ , with  $|\lambda| < 1$
3. a positive real eigenvalue  $\lambda$ , with  $|\lambda| > 1$
4. a pair of complex conjugate eigenvalues  $\lambda_i$ , with  $|\lambda_i| > 1$

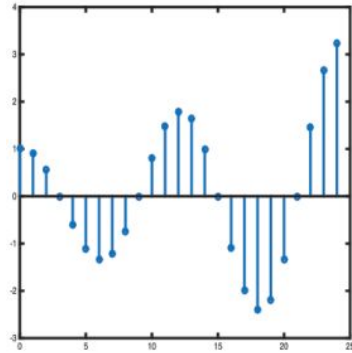
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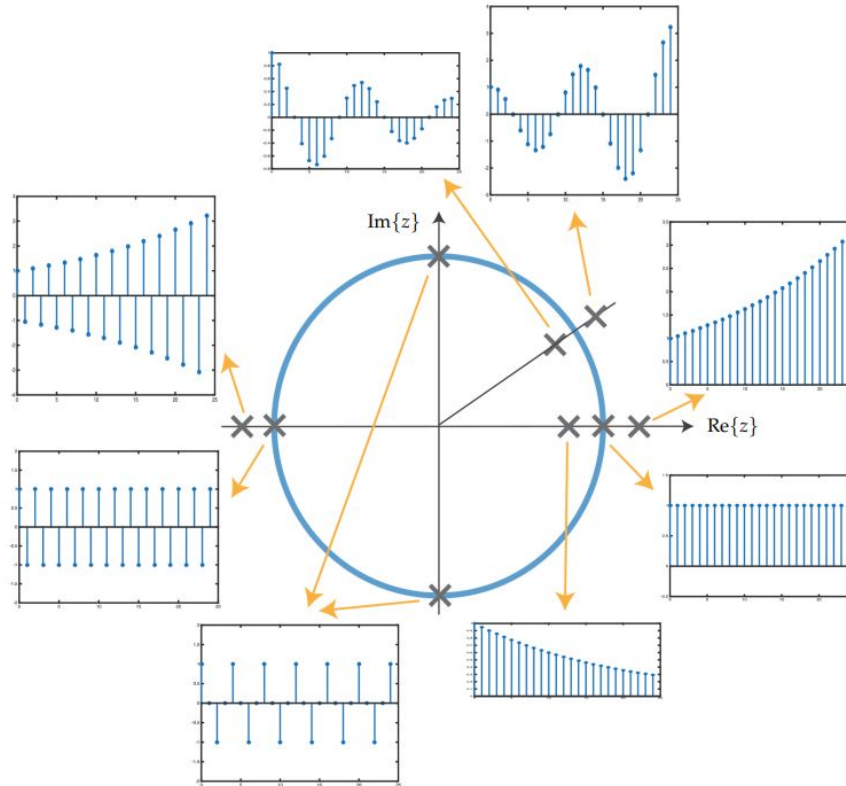
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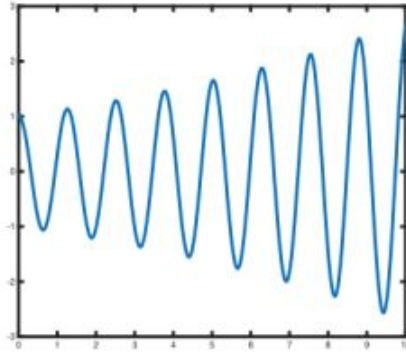
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# Stability - Eigenvalues for DT System



note: only the real part of the response is shown

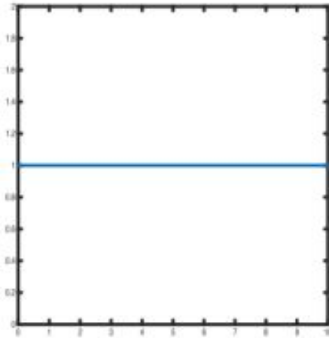
A real-valued CT system generates the following state trajectory:



The above response is associated with which of the following:

1. a real eigenvalue  $\lambda$ , with  $\lambda < 0$
2. an eigenvalue  $\lambda$  at the origin ( $\lambda = 0$ )
3. a pair of complex conjugate eigenvalues  $\lambda_i$ , with  $|\lambda_i| > 1$
4. a pair of complex conjugate eigenvalues  $\lambda_i$ , with  $\text{Re}\{\lambda_i\} > 0$

A real-valued CT system generates the following state trajectory:

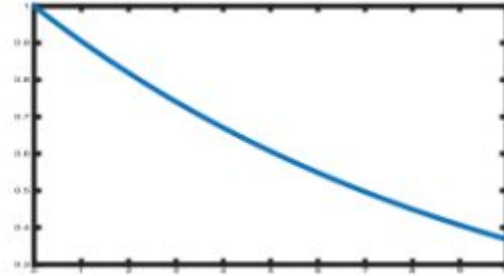


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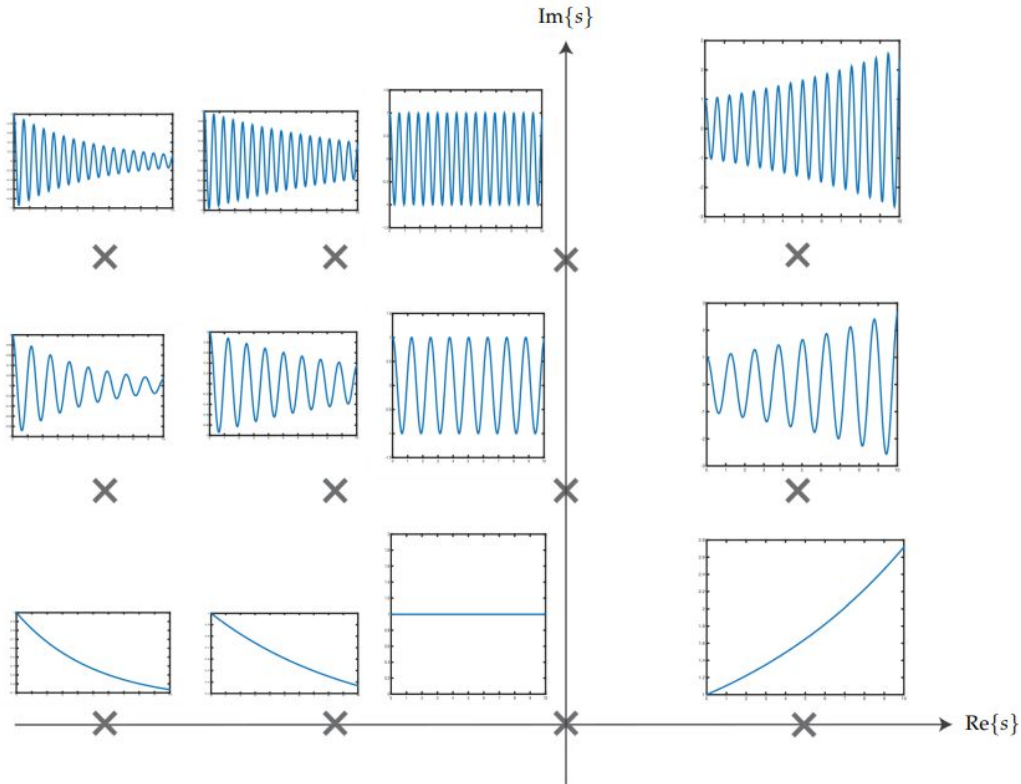
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# Stability - Eigenvalues for CT System



note: only the real part of the response is shown

# Feedback Stabilization



“fly-by-wire”  
(electronic feedback control)

# Controllability

